## Second Semester M.Tech. Degree Examination, June/July 2016 Synthesis and Optimization of Digital Circuits

Time: 3 hrs. Max. Marks: 100

Note: Answer any FIVE full questions.

1 a. Explain the different microelectronic design styles.

(08 Marks)

b. Explain surjective, injective and bijective functions.

(06 Marks)

c. Define (i) Polar dag (ii) Acyclic graph(v) Indegree & Outdegree.

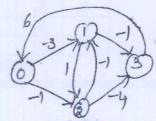
(iv) Complete graph

(1) magnet & outdegree.

(06 Marks)

2 a. Find the shortest path for the graph shown in Fig. Q2 (a) using Bellman-Ford algorithm.

(10 Marks)



(iii) Cutset

Fig. Q2 (a)

- b. For the function, f = ab + bc + ac, compute the expansion on the orthonormal basis. Given that  $\phi_1 = a$ ,  $\phi_2 = a'b$  and  $\phi_3 = a'b'$ . Consider the lower bound of  $f_{\phi_1}$  in each case. (10 Marks)
- 3 a. Consider the following equations:

$$x_1 = x + dx$$
;

$$U_1 = [U - (3 * x * u * dx) - (3 * y * dx)];$$

$$y_1 = (y + u * dx);$$

$$c = x_1 < a$$
;

$$x = x_1$$
;  $u = u_1$ ,  $y = y_1$ 

Implement in VHDL using behavior style. The input and output port signals are of integer and the range is from 0 to 255. (10 Marks)

- b. Explain tree height reduction, constant propagation, dead code elimination, operator strength reduction and loop expansion. (10 Marks)
- 4 a. For the function f(a,b,c) = a'c' + a'b + bc + ac and  $f_2(a,b,c) = bc$ , obtain the cover of the function, minimum cover and irredundant cover. Represent the same in Boolean cube.

(10 Marks)

- b. Represent the function, f = ab + ac + ab'c' + a' in positional cube rotation and check the function is tautology or not. (10 Marks)
- 5 a. Find the expanded cover of the function f = a'b'c' + ab'c' + a'bc' + a'bc' with abc' as a don't care condition. (08 Marks)
  - b. Draw the logic network after elimination and decomposition described with primary input variables {a, b, c, d, e} and primary output variables {w, x, y, z} by the combinational equations:

$$p = ce + de$$
;  $q = a + b$ ;  $r = p + a'$ ;  $s = r + b'$ ;  $t = ac + ad + bc + bd + e$ ;  $u = q'c + qc' + qc$ ,  $v = a'd + bd + c'd + ae'$ ,  $w = v$ ,  $x = s$ ,  $y = t$ ,  $z = u$ . (12 Marks)

6 a. Find the kernel set of f = ace + bce + de + g. Also find its co-kernel.

(10 Marks)

- b. For the expression, f = ace + bce + de + g, write the corresponding matrix representation. Also find the rectangles and its co-rectangles. (10 Marks)
- 7 a. Explain the state encoding for two level circuits using the state table given in table Q7 (a).

(10 Marks)

Input	State	Next state	Output
0	$S_1$	$S_3$	0
1	$S_1$	$S_3$	0
0	S <sub>2</sub>	$S_3$	0
1	$S_2$	$S_1$	1
0	$S_3$	$S_5$	0
1	$S_3$	S <sub>4</sub>	1
0	S <sub>4</sub>	$S_2$	1
1	S <sub>4</sub>	$S_3$	0
0	$S_5$	$S_2$	D
1	$S_5$	S <sub>5</sub>	0

Table Q7 (a)

- b. Explain modeling and assumption for retiming in sequential circuit optimization using network models. (10 Marks)
- 8 a. Explain integer linear programming model of scheduling with resource constraints.

(10 Marks)

b. Briefly explain rule based library binding.

(10 Marks)